

# Celebration of $\pi$ Approximation Day at Palanghat Cluster under Narsingpur Elementary Education, Cachar, Assam

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$\pi$  is a mathematical constant approximately equal to 3.14159....  $\pi$  is defined in Euclidean Geometry as the ratio of the circumference of a circle to its diameter. Although  $\pi$  is an irrational number,  $\pi$  Approximation Day is observed on 22nd July, since the fraction  $22/7$  is a common approximation of  $\pi$  which is accurate to two decimal places. This day is observed annually to celebrate the usage of the mathematical constant  $\pi$ .

This year a program was conducted in online mode and was presided over by me on the occasion of  $\pi$  Approximation Day. On this occasion, the students of Palanghat Cluster drew pictures of the constant in their homes. Also an online Mathematics Quiz was conducted to make the subject interesting among the students. The competition was conducted in two categories. Students of class 8 and 9 participated in the 1st category. The 2nd category was for the students of class 10 and 11.

About 110 students participated in both the categories. The 1st, 2nd and 3rd Rank holders of both the categories were awarded a memorial award, certificate and a letter of appreciation and all the participants received e-certificate of participation.

In the 1st category of class 8 and 9, the prizes were awarded to the following students:

- 1) Harshita Deb of class 8, Vivekananda Kendra Vidyalaya, Borojalenga, Cachar, secured the 1st position and Late Minu Roy Memorial Award, with the courtesy of Bikash Roy (Assistant Teacher), Nageshwar Tilla Pt-2 L.P. School, Rukni, Cachar, Assam was awarded to her.
- 2) Debolina Das of class 8, Ideal Home English Medium High School, Ramkrishna Nagar, Karimganj, secured the 2nd position and Late Sumanta Kr. Das Memorial Award,

with the courtesy of Nilendu Kr. Das (Assistant Teacher), 604 No. Barodalu L.P. School Palanghat, Cachar, Assam was awarded to her.

- 3) Anubhav Roy of class 8, Vivekananda Kendra Vidyalaya Borojalenga, Cachar, secured the 3rd position and Late Tufan Paul Memorial Award, with the courtesy of Pronoy Paul, Assistant Teacher cum C.R.C.C., Palanghat, Cachar Assam was awarded to him.

In the second category of Class- 10 and 11, the prizes were awarded to the following students:

- 1) Himadri Dey of class 10, Oriental High School, Silchar secured the 1st position and Late Satyabati Dey Memorial Award, with the courtesy of M/S Rajarshi Medicos Chemist and Druggist, Lalganesh Guwahati was awarded to him.
- 2) Siddharth Paul of class 10, Ramanuj Vidya Mandir, secured the 2nd position and Late Ram Prosad Nunia Memorial Award, with the courtesy of Pradip Kr. Nunia (Hindi Teacher), Palanghat M.V. School, Cachar, Assam was awarded to him.
- 3) Manish Paul of class 10, Ramanuj Vidya Mandir, secured the 3rd position and Late Geeta Paul Memorial Award, with the courtesy of Pronoy Paul Assistant Teacher cum C.R.C.C. Palanghat, Cachar, Assam was awarded to him.

Thanks to all the participants for their active participation and sincere thanks to all teachers, parents and media for their valuable contribution for making the event a grand success. We look forward to organise such events in the future. Below we present the questions asked in the quiz contest.

## Questions

### Section A

1. 'X', an ancient Indian mathematician gave the value of  $\pi$  as  $62832/20000$ , which is equal to 3.1416 (correct upto four decimal places) and also mentioned that this value of  $\pi$  is approximate ("asanna"). Identify 'X'.

(A) Ramanujan

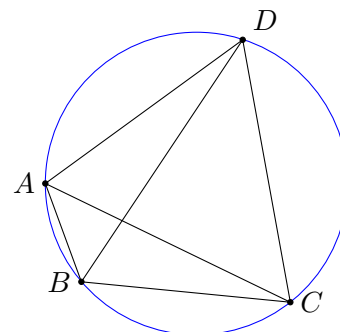
(B) Brahmagupta

(C) Madhava

(D) Aryabhata

(E) Lilabati

2. The theorem related to this figure is  $AC \cdot BD = AB \cdot CD + BC \cdot AD$ . The theorem was given by:



(A) Brahmagupta

(B) Ptolemy

(C) Ceva

(D) Menelaus

(E) Thales

3. Which one of the following is a wrong statement?

(A) Pi( $\pi$ ) Approximation Day on July 22 honours the concept of pi( $\pi$ )

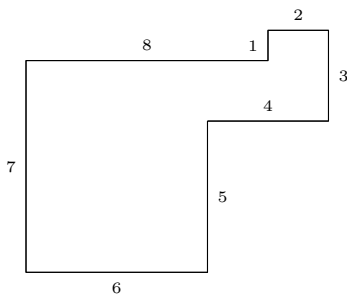
(B) Pi( $\pi$ ) is occasionally referred to as the Archimedes constant

(C) Pi( $\pi$ ) is transcendental

(D) Pi( $\pi$ ) is equal to the ratio of two numbers 22 and 7 which makes it an irrational number

(E) In the approximate value of pi( $\pi$ ) the digits in the decimal part go on and on with no pattern, neither ends nor repeats

4. A 'X' is any polygon (see diagram below) with all right angles whose sides are consecutive integer lengths. Identify 'X'.



(A) Polygon

(B) Octagon

(C) Golygon

(D) Decagon

(E) Heptagon

5. 'X' was an Indian scientist and statistician who had a significant role in formulating India's strategy for industrialization in the 2nd Five-Year Plan (1956-61). 'X' was the founder of the reputed Indian Statistical Institute. 'X' was also a friend of Srinivasa Ramanujan at Cambridge. Identify 'X'.

(A) P.C. Ray

(B) P.C. Mahalanobis

(C) C.R. Rao

(D) C.S. Seshadri

(E) S.N. Bose

6. Below is an image of a surveying instrument which works on the principle of trigonometry. It is used for measuring angles with the help of a rotating telescope. Identify the instrument

(A) Ammeter

(B) Protractor

(C) Anemometer

(D) Theodolite

(E) Gauge

7. 'X' was an ancient Indian mathematician, who was a Vedic brahmin priest and an architect of very high standards. He stated the theorem now known as Pythagoras theorem in his book Sulbha Sutra. The picture of 'X' is given below. Identify 'X'.

(A) Sridhar Acharya

(B) Aryabhatta

(C) Brahmagupta

(D) Baudhayana

(E) Bhaskara

8. "Every even integer greater than 2 can be ex-

pressed as a sum of two primes". It is known as:

- (A) Hodge conjecture
- (B) Twin prime conjecture
- (C) Legendre's conjecture
- (D) Andrica's conjecture
- (E) Goldbach's conjecture

9. Suppose we are going to prove that a statement  $p$  is true, we firstly assume that the negation of the statement is true i.e.,  $\sim p$  is true. Then we prove that  $\sim p$  is false. Hence the statement  $p$  is true. What is this method of proof called?

- (A) Method of induction
- (B) Method of substitution
- (C) Method of elimination
- (D) Method of contradiction
- (E) Method of partial fractions

10. Regarded as the highest honour in the field of mathematics, the 'X' is a prize awarded to two, three or four mathematicians every four years by the International Mathematical Union(IMU). It was first awarded to the Finnish mathematician Lars Ahlfors in 1936 and it has been awarded every four years since 1950. This prize has only one female recipient. Identify the prize 'X'.

- (A) Abel Prize
- (B) Fields Medal

(C) Chern Medal

(D) Nobel Prize

(E) Wolf Prize

## Section B

1. If  $2^a = 3^b = 7^c = 42$ , then what is the value of  $\frac{1}{a} + \frac{1}{b} + \frac{1}{c}$ ?

(A) 1

(B) 2

(C) 3

(D) 4

(E) 5

2. The average score of boys in an examination of a school is 71 and that of girls is 73. The average score of the school in the examination is 71.8. Find the ratio of the number of boys to the number of girls that appeared in the examination.

(A) 3:2

(B) 2:3

(C) 3:4

(D) 4:3

(E) 1:2

3. We write down all the digits from 1 to 9 side by side. Now we put '+' between as many digits as we wish to, so that the sum of the numbers become 513. It is explained below

1    2    3    4    5    6    7    8    9

= 513

Now suppose we put '+' signs at the following places:

$12+345+67+89=513$

Since there are four numbers, so the average can be calculated by dividing the sum by 4. What is the average, if the sum is 261?

(A) 52.2

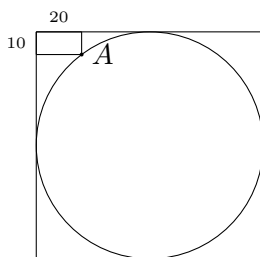
(B) 42.2

(C) 62.2

(D) 72.2

(E) 32.2

4. In the figure given below, the rectangle at the corner measure  $20\text{ cm} \times 10\text{ cm}$ . The corner  $A$  of the rectangle is also a point on the circumference of the circle. What is the radius of the circle in cm?



(A) 10

(B) 40

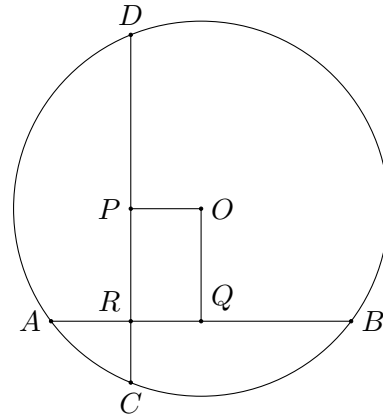
(C) 50

(D) 60

(E) none of the above

5.  $AB$  and  $CD$  are mutually perpendicular

chords of a circle intersecting at a point  $R$  (see figure).  $OP$  and  $OQ$  are perpendiculars on chords  $CD$  and  $AB$  respectively. If  $OP = 1$ ,  $OQ = 4$  and  $DP = 2BQ$ , then what is the approximate value of  $AB$ ? (figure not to scale)



(A) 1.732

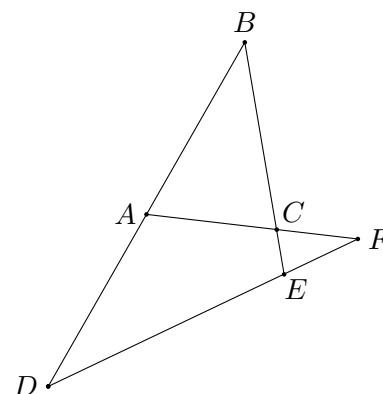
(B) 2.236

(C) 2.828

(D) 3.464

(E) 4.472

6. In the figure below,  $BAD$ ,  $BCE$ ,  $ACF$  and  $DEF$  are straight lines. If  $BA = BC$ ,  $AD = AF$ ,  $EB = ED$  and  $\angle BED = x^\circ$ , then what is the value of  $x$ ?



(A) 96

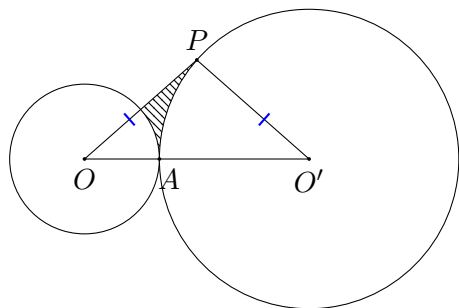
- (B) 102
- (C) 108
- (D) 115
- (E) 120
7. A lady goes to 3 different temples for performing puja with 'X' flowers but she needs to offer 'Y' flowers to the idols in each temple. She goes to a magical pond that can double the number of flowers washed in it. She washes the 'X' flowers, doubles it and offers 'Y' flowers among them to the 1st temple. Then she goes to the pond again, doubles the remaining flowers and offers 'Y' among them to the 2nd temple. Again she doubles the remaining flowers and after offering 'Y' flowers to the 3rd temple, her task is accomplished and she has no flowers remaining with her. What could be the possible values of 'X' and 'Y'?
- (A) 5 and 6
- (B) 6 and 5
- (C) 6 and 7
- (D) 7 and 6
- (E) 7 and 8
8. The product of three integers X, Y and Z is 192. Given that Z is equal to 4 and P is equal to the average of X and Y. What is the minimum possible value of P?
- (A) 6
- (B) 6.5
- (C) 7
- (D) 8
- (E) 9.5
9. Given that the positive integers  $x > 1$  and  $y$  satisfies the equation  $2007x - 21y = 1923$ . Find the minimum value of  $3x + 2y$ .
- (A) 1342
- (B) 1370
- (C) 2013
- (D) 2021
- (E) 2035
10. If  $x$  is a real number and
- $$A = \frac{-1 + 3x}{1 + x} - \frac{\sqrt{|x| - 2} - \sqrt{2 - |x|}}{|2 - x|}$$
- then what is the value of  $A$ ?
- (A) 3
- (B) 5
- (C) 7
- (D) 9
- (E) 11

## Section C

1. Find the number of positive integral values of  $n$  for which  $n^2 + 96$  is a perfect square.
- (A) 0
- (B) 1
- (C) 2

- (D) 3
- (E) 4
2.  $1011 \left[ 1 + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+\dots+2021} \right] = ?$
- (A) 2019
- (B) 2020
- (C) 2021
- (D) 2022
- (E) 2023
3. How many triplets of prime numbers  $(p, q, r)$  satisfy the equation
- $$15p + 7pq + qr = pqr$$
- (A) 0
- (B) 1
- (C) 2
- (D) 3
- (E) 4

4. Two circles with centres  $O$  and  $O'$  intersect at a point  $A$  such that  $OA = \sqrt{2} - 1$ . If  $OP$  is a tangent to the circle with centre  $O'$  and  $OP = O'P$ , then find the approximate area of the shaded region.



- (A) 0.6
- (B) 0.3
- (C) 0.04
- (D) 0.03
- (E) 0.02
5. The diagonals of a square tile are painted symmetrically with a brush of width 1 unit as shown in the figure. Exactly half of the area of this tile is covered with paint. What is the length of the side of this tile?
- (A)  $\sqrt{2} - 2$
- (B)  $\sqrt{2} - 1$
- (C)  $\sqrt{2}$
- (D)  $\sqrt{2} + 1$
- (E)  $\sqrt{2} + 2$

## Hints and Solutions

### Section A

1. (D)
2. (B)
3. (D)
4. (C)
5. (B)
6. (D)
7. (D)
8. (E)
9. (D)
10. (B)

## Section B

1. (A)

Given,  $2^a = 3^b = 7^c = 42$ . Therefore,  $42^{\frac{1}{a}} = 2$ ,  $42^{\frac{1}{b}} = 3$ ,  $42^{\frac{1}{c}} = 7$ . Multiplying, we get  $42^{\frac{1}{a}} \cdot 42^{\frac{1}{b}} \cdot 42^{\frac{1}{c}} = 2 \cdot 3 \cdot 7$ , or,  $42^{\frac{1}{a} + \frac{1}{b} + \frac{1}{c}} = 42$  or,  $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 1$ .

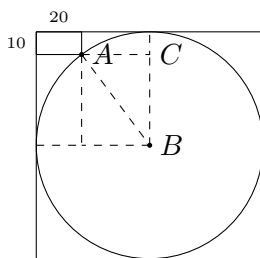
2. (A)

Let the number of boys be  $x$  and the number of girls be  $y$ . Given, average score of boys = 71,  $\therefore$  total score of boys =  $71x$ . Average score of girls = 73,  $\therefore$  total score of girls =  $73y$ . Now, Average score =  $\frac{\text{Total score}}{\text{Total no. of students}}$  or,  $71.8 = \frac{71x + 73y}{x + y}$ . Solving we get  $8x = 12y \Rightarrow x : y = 3 : 2$ .

3. (A)

261 is possible only if we take  $123 + 45 + 6 + 78 + 9$ . So, average will be  $\frac{261}{5} = 52.2$ .

4. (C)



Let the radius be  $AB = r$ , then  $AC = r - 20$  and  $BC = r - 10$ . Therefore, by the Pythagoras theorem in  $\triangle ABC$ , we have  $AC^2 + BC^2 = AB^2$ , i.e.,  $(r - 20)^2 + (r - 10)^2 = r^2$ . Solving we get  $r^2 - 60r + 500 = 0 \Rightarrow (r - 50)(r - 10) = 0$ . Therefore,  $r = 50$  or  $r = 10$ . Note that  $r$  would be 10 if the corner of the rectangle had been lying on the inner circumference. But as per the given figure, the radius of the circle should be 50 cm.

5. (E)

Let  $BQ = x$  and  $DP = 2x$ . Clearly,  $OPRQ$  is a rectangle and hence  $PR = OQ = 4$  and  $OP = QR = 1$ . Since perpendicular drawn from centre to a chord also bisects the chord, therefore  $DP = CP = 2x$  and  $AQ = BQ = x$ . Hence,  $DR = DP + PR = 2x + 4$ ,  $CR = CP - PR = 2x - 4$ ,  $BR = BQ + QR = x + 1$ ,  $AR = AQ - QR = x - 1$ .

By Intersecting Chords Theorem,  $AR \cdot BR = CR \cdot DR \Rightarrow (x - 1)(x + 1) = (2x - 4)(2x + 4) \Rightarrow x^2 - 1 = 4x^2 - 16 \Rightarrow 3x^2 = 15 \Rightarrow x = \sqrt{5}$ . Therefore,  $AB = 2x = 2\sqrt{5} = 4.472$  (approx.).

6. (C)

Let  $\angle ADF = \alpha$ . Since  $AD = AF$ , therefore  $\angle ADF = \angle AFD = \alpha$ . So,  $\angle BAC = \angle ADF + \angle AFD = 2\alpha$ . Since  $BA = BC$ , therefore  $\angle BAC = \angle BCA = 2\alpha$ . So,  $\angle ABC = 180^\circ - 4\alpha$ . Also since  $EB = ED$ , therefore  $\angle EBD = \angle EDB \Rightarrow 180^\circ - 4\alpha = \alpha \Rightarrow 5\alpha = 180^\circ \Rightarrow \alpha = 36^\circ$ . Hence,  $\angle BED = 180^\circ - 2\alpha = 180^\circ - 72^\circ = 108^\circ$ . So,  $x = 108$ .

7. (E)

$7 \times 2 - 8 = 14 - 8 = 6$ ,  $6 \times 2 - 8 = 12 - 8 = 4$ ,  $4 \times 2 - 8 = 8 - 8 = 0$ .

So she had  $X = 7$  flowers initially and had offered  $Y = 8$  flowers in each temple.

8. (C)

Given that the product of three integers  $X$ ,  $Y$  and  $Z$  is 192. Also  $Z = 4$  and  $P = \frac{X+Y}{2}$ . Now,  $XYZ = 192 \Rightarrow XY \cdot 4 = 192 \Rightarrow XY = 48 = 1 \times 48 = 2 \times 24 = 3 \times 16 = 4 \times 12 = 6 \times 8$ . Also given  $P = \frac{X+Y}{2}$ .  $(X, Y) = (1, 48) \Rightarrow P = \frac{1+48}{2} = \frac{49}{2} \notin \mathbb{Z}$



$$(X, Y) = (2, 24) \Rightarrow P = \frac{2+24}{2} = 13 \in \mathbb{Z}$$

$$(X, Y) = (3, 16) \Rightarrow P = \frac{3+16}{2} = \frac{19}{2} \notin \mathbb{Z}$$

$$(X, Y) = (4, 12) \Rightarrow P = \frac{4+12}{2} = 8 \in \mathbb{Z}$$

$$(X, Y) = (6, 8) \Rightarrow P = \frac{6+8}{2} = 7 \in \mathbb{Z}$$

$\therefore$  Minimum possible value of P is 7.

9. (B)

Given equation is  $2007x - 21y = 1923$ .

Dividing by 3, we have

$$669x - 7y = 641 \Rightarrow 669x - 7y = 669 - 28 \Rightarrow$$

$$669(x - 1) = 7(y - 4)$$

Therefore,  $x$  and  $y$  will be minimum if  $x - 1 = 7$  and  $y - 4 = 669$  i.e.,  $x_{\min} = 8$  and  $y_{\min} = 673$ . Therefore,  $(3x + 2y)_{\min} = 3 \times 8 + 2 \times 673 = 1370$ .

10. (C)

Since  $|x| - 2$  and  $2 - |x|$  are inside square roots, so  $|x| - 2 \geq 0$  and  $2 - |x| \geq 0$  simultaneously. Thus,  $|x| = 2 \Rightarrow x = \pm 2$ . If  $x = 2$ , then the denominator of 2<sup>nd</sup> term (i.e.,  $|2 - x|$ ) becomes 0, which is not possible. Hence,  $x = -2$  only. Putting  $x = -2$  in the given expression, we have  $A = 7$ .

## Section C

1. (E)

Let  $n^2 + 96 = m^2$ , where  $m \in \mathbb{Z}$ . This implies  $m^2 - n^2 = 96$ , or,  $(m - n)(m + n) = 96 = 2 \times 48 = 3 \times 32 = 4 \times 24 = 6 \times 16 = 8 \times 12$ . If  $m - n = 2, m + n = 48$ , solving we get  $n = 23 \in \mathbb{Z}$ . If  $m - n = 3, m + n = 32$ ,

solving we get  $n = \frac{29}{2} \notin \mathbb{Z}$ . If  $m - n = 4, m + n = 24$ , solving we get  $n = 10 \in \mathbb{Z}$ . If  $m - n = 6, m + n = 16$ , solving we get  $n = 5 \in \mathbb{Z}$ . If  $m - n = 8, m + n = 12$ , solving we get  $n = 2 \in \mathbb{Z}$ . Hence there are four values of  $n$  (2, 5, 10 and 23) for which  $n^2 + 96$  is a perfect square.

2. (C)

$$\begin{aligned} & 1 + \frac{1}{1+2} + \frac{1}{1+2+3} + \dots + \frac{1}{1+2+\dots+2021} \\ &= \sum_{n=1}^{2021} \frac{1}{1+2+\dots+n} \\ &= \sum_{n=1}^{2021} \frac{1}{\frac{n(n+1)}{2}} \\ &= 2 \sum_{n=1}^{2021} \frac{1}{n(n+1)} \\ &= 2 \sum_{n=1}^{2021} \frac{(n+1) - n}{n(n+1)} \\ &= 2 \sum_{n=1}^{2021} \left( \frac{1}{n} - \frac{1}{n+1} \right) \\ &= 2 \left[ 1 - \frac{1}{2022} \right] = 2 \times \frac{2021}{2022}. \end{aligned}$$

Therefore required result is  $1011 \times 2 \times \frac{2021}{2022} = 2021$ .

3. (D)

The given equation can be written as  $qr = p(qr - 79 - 15)$ . Since  $p, q, r$  are all primes, so there arise two cases:

**Case 1:** Considering  $p = q$ , we have  $r = qr - 7q - 15 \Rightarrow qr - 7q - r = 15 \Rightarrow q(r - 7) - (r - 7) = 15 + 7 \Rightarrow (q - 1)(r - 7) = 22$ . Now, 22 can be factored as  $1 \times 22 = 22 \times 1 = 2 \times 11 = 11 \times 2$ . So we get  $q = 2, r = 29$  or  $q = 23, r = 8$  or  $q = 3, r = 18$  or  $q = 12, r = 9$  but since  $q, r$  are primes, so only  $q = 2, r = 29$  is possible. Thus,  $p = q = 2$ . Hence, one such triplet is  $(p, q, r) = (2, 2, 29)$ .

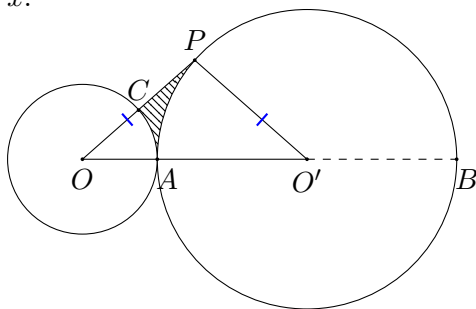
**Case 2:** Considering  $p = r$ , we have  $q =$

$qr - 7q - 15 \Rightarrow qr - 8q = 15 \Rightarrow q(r - 8) = 15$ .  
 Now 15 can be factored as  $1 \times 15 = 15 \times 1 = 3 \times 5 = 5 \times 3$ . So we get  $q = 1, r = 23$  or  $q = 15, r = 9$  or  $q = 3, r = 13$  or  $q = 5, r = 11$  but since  $q, r$  are primes, so only  $q = 3, r = 13$  and  $q = 5, r = 11$  are possible. Using  $p = r$ , two more triplets are  $(p, q, r) = (13, 3, 13), (11, 5, 11)$ .

Therefore, there are **3** triplets of primes  $(p, q, r)$  satisfying the equation  $15p + 7pq + qr = pqr$ .

4. (C)

Extend  $AO'$  to intersect the circle at  $B$ . Let the point of intersection of  $OP$  and the circle with centre  $O$  be  $C$ . Let  $O'A = O'P = OP = x$ .



By tangent-secant theorem,  
 $OP^2 = OA \cdot OB$

$$\begin{aligned} \Rightarrow x^2 &= (\sqrt{2} - 1)(\sqrt{2} - 1 + 2x) \\ \Rightarrow x^2 &= (\sqrt{2} - 1)^2 + 2x(\sqrt{2} - 1) \\ \Rightarrow x^2 - 2x(\sqrt{2} - 1) + (\sqrt{2} - 1)^2 &= 2(\sqrt{2} - 1)^2 \\ \Rightarrow \{x - (\sqrt{2} - 1)\}^2 &= 2(\sqrt{2} - 1)^2 \\ \Rightarrow x - (\sqrt{2} - 1) &= \sqrt{2}(\sqrt{2} - 1) \\ \Rightarrow x - \sqrt{2} + 1 &= 2 - \sqrt{2} \\ \Rightarrow x &= 1 \end{aligned}$$

Therefore, area of  $\triangle OO'P = \frac{1}{2}x^2 = \frac{1}{2}(1)^2 = \frac{1}{2}$  sq. units. Since  $OP = O'P$  and  $OP$  is a tangent, i.e.,  $\angle OPO' = 90^\circ$ , so  $\angle POO' = \angle PO'O = 45^\circ$ . Therefore, the areas of sectors  $OAC$  and  $O'AP$  are  $\frac{45}{360} = \frac{1}{8}$  times the areas of their respective circles. So, area of shaded region

$$\begin{aligned} &= \text{ar}(\triangle OO'P) - \{\text{ar}(\text{sector } OAC) + \text{ar}(\text{sector } O'AP)\} \\ &= \frac{1}{2} - \frac{1}{8}\pi\{(\sqrt{2} - 1)^2 + 1^2\} \\ &= \frac{1}{2} - \frac{1}{8}\pi(4 - 2\sqrt{2}) \\ &= 0.04 \text{ (approx.)} \end{aligned}$$

5. (D)

Let  $DE = x$  and  $EG = y$ . By the Pythagoras theorem,  $1^2 = x^2 + x^2 = 2x^2 \Rightarrow x = \frac{1}{\sqrt{2}}$ ,  
 $EF = CD - 2DE = CD - 2 \times \frac{1}{\sqrt{2}} = CD - \sqrt{2}$ .  
 Now,  $EF^2 = EG^2 + GF^2 = y^2 + y^2$ . Therefore,  $(CD - \sqrt{2})^2 = 2y^2$ .

$$\begin{aligned} \Rightarrow CD - \sqrt{2} &= \sqrt{2}y \\ \Rightarrow y &= \frac{CD - \sqrt{2}}{\sqrt{2}} \end{aligned}$$

According to question, Area of shaded region = Area of unshaded region =  $\frac{1}{2}$ (Area of square)

$$\begin{aligned} \Rightarrow 4\left(\frac{1}{2}y^2\right) &= \frac{1}{2}CD^2 \\ \Rightarrow CD &= 2y = 2 \cdot \frac{CD - \sqrt{2}}{\sqrt{2}} \\ \Rightarrow CD &= \sqrt{2}CD - 1 \\ \Rightarrow (\sqrt{2} - 1)CD &= 1 \end{aligned}$$

$\Rightarrow CD = \frac{1}{\sqrt{2} - 1} = \sqrt{2} + 1$  units is the length of the tile.